

CCSU  
DEPARTMENT OF MATHEMATICAL SCIENCES

# COLLOQUIUM

Friday, March 27

3:00 – 4:00 PM

Maria Sanford, Room 101

## SOME MATHEMATICS OF PYTHAGOREAN TRIPLES

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**Abstract:** A Pythagorean triple are three integers,  $(a, b, c)$ , that satisfy  $a^2 + b^2 = c^2$ . For example,  $3^2 + 4^2 = 9 + 16 = 25 = 5^2$ . If  $a, b, c$  are relatively prime, the triple is called *primitive*. This talk discusses some properties of primitive triples featuring the following. First, proving that they all have the form  $(r^2 - s^2, 2rs, r^2 + s^2)$  for integers,  $r, s$ . Second, radially projecting triples onto a unit circle produces a bijection with the rational points on it. Third, representing these rational points in the form  $e^{i\theta}$ , there is a group isomorphism between triples and complex multiplication of rational, unit complex numbers. Last, showing the connection between primes of the form  $p = a^2 + b^2$  and finding a triple where  $c = p$ . A computational example is done for  $p = 1,000,000,021$  using Python. If you love integers, this talk is for you.

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For further information: [gotchevi@ccsu.edu](mailto:gotchevi@ccsu.edu); 860-832-2839; <http://mathcolloquium.sites.ccsu.edu/>